



# CAPTURING THE OFF-AXIS BEHAVIOR OF THIN-PLY LAMINATES

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# Why thin-ply composites?

- High Versatility
- Tailored design
- Superior **strength to weight ratio**



*Thin-ply  
composites made  
it to and flew on  
Mars in 2021*

*The ACS3 spacecraft  
will showcase the  
ability to use composite  
deployable booms*



# What's new...

## The difference

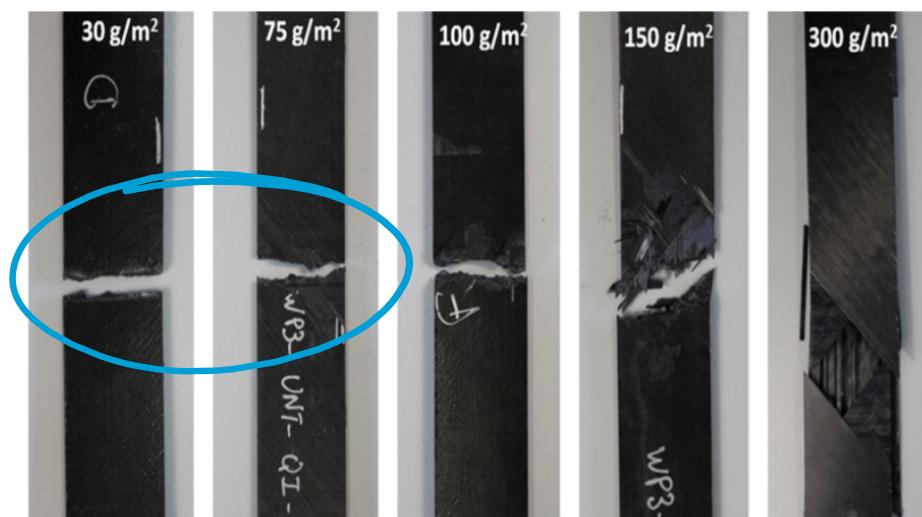
Ply thickness  $\geq 100 \mu\text{m}$

~~Matrix dominated  
and  
Fiber dominated~~



~~Interlaminar  
and  
Intralaminar~~

Ply thickness  $\leq 100 \mu\text{m}$



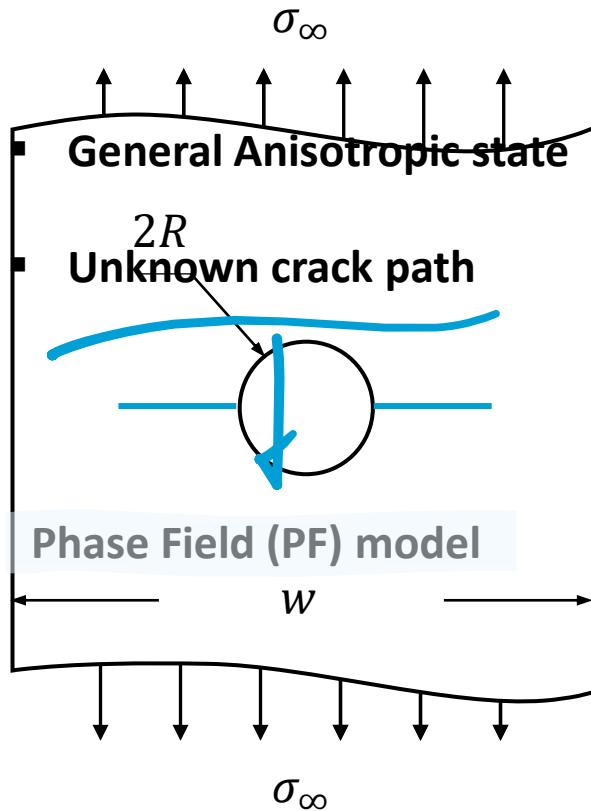
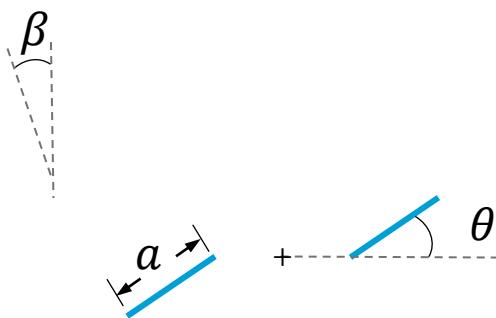
Amacher et al. (2014)

## Options

An **Equivalent Single Layer (ESL) approach** seems fit.

# The problem

A simple problem: **Open Hole Tension**



Elastic

Proper representation of the material at the ESL level:

- Macro-mechanical homogenization effects. ( $[A]=[D]$ ,  $[B]=0$ )
- CLPT or other continuum approaches can represent the material with a homogenized compliance matrix

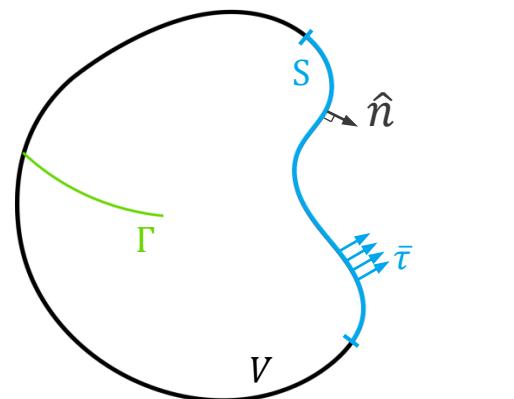
$$\boldsymbol{\varepsilon} = \mathbf{S}\boldsymbol{\sigma} \text{ or } \boldsymbol{\sigma} = \mathbf{C}\boldsymbol{\varepsilon}$$

Fracture

How can directional toughness be defined ?

# PF in a nutshell

It is a method relies on the **total potential energy minimization** linked to the variational expression of Griffith's energy balance.

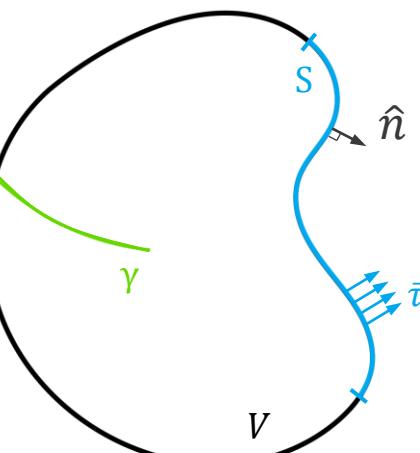


$$\Pi(u) = U_e + U_f - W$$

$$U_f = \int_{\Gamma} G_c d\Gamma$$



$$U_e = g(\varphi) \int_V \frac{1}{2} C \epsilon^2 dV$$



$$U_f = \int_{\Gamma} G_c d\Gamma \approx \int_V g_c \gamma(\varphi, \nabla \varphi) dV$$

The PF variable acts like a damage variable:

$\varphi = 0$  undamaged state

$\varphi = 1$  damaged state

crack surface density function

Governing equations:

$$\nabla \sigma = 0 \quad \text{in } V$$

$$\nabla \cdot \left( \frac{\partial U}{\partial \nabla \varphi} \right) - \frac{\partial U}{\partial \varphi} = 0 \quad \text{in } S$$

Evolution equation

# Incorporating Fracture Energy Anisotropy

The crack surface density function:

$$\gamma(\varphi, \nabla\varphi) = \frac{1}{2l} \left( \varphi^2 - \frac{l}{2} \nabla\varphi \cdot \mathbf{A} \cdot \nabla\varphi \right)$$

*length scale*

*structural tensor*

$$\mathbf{A} = 1 + a_1 \mathbf{a}_1 \otimes \mathbf{a}_1 + a_2 \mathbf{a}_2 \otimes \mathbf{a}_2$$

*scaling constants*

The new toughness:

$$G_c(\theta) = g_c \sqrt{\frac{l^*}{l}}$$

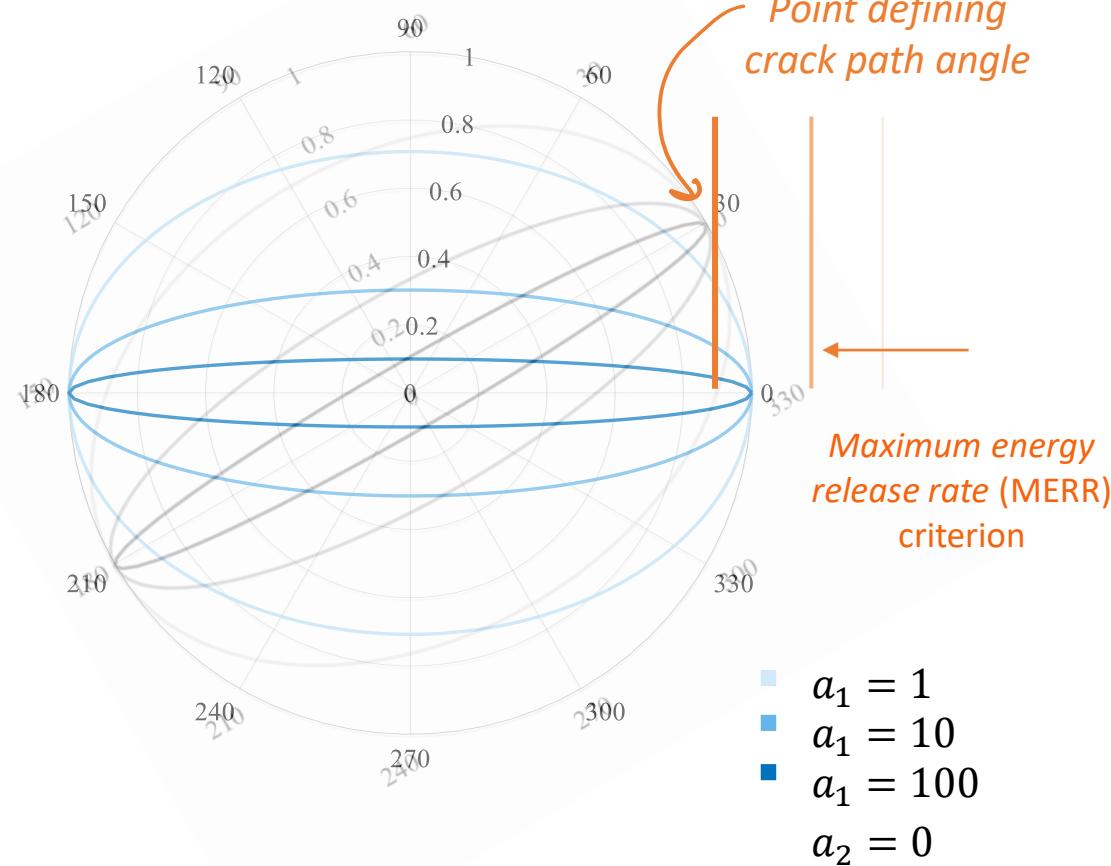
*effective length scale*

$$l^* = l(1 + a_1 \sin^2(\theta) + a_2 \cos^2(\theta))$$

*Angle of crack with respect to the preferred  $\mathbf{a}_1$  direction*

$$G_c(\theta) = g_c \sqrt{1 + a_1 \sin^2(\theta) + a_2 \cos^2(\theta)}$$

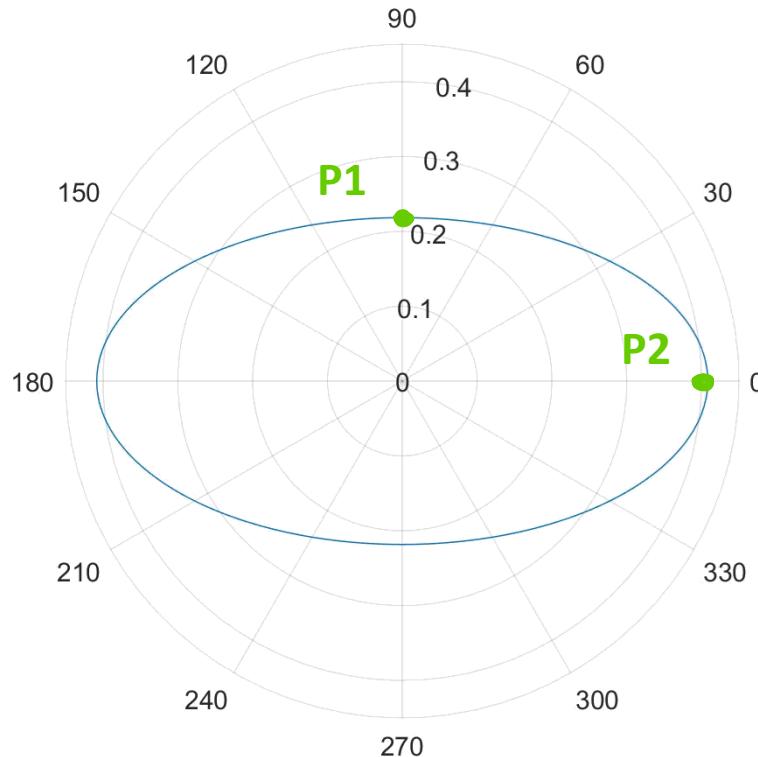
Inverse toughness,  $G_c(\theta)^{-1}$ , plot:



# The “proper” scaling constants

If the path is **unknown or a predefined link to a direction exists**, then the toughness distribution will produce the crack angle as an output...

**Inverse toughness:**



$$G_c(\theta) = g_c \sqrt{1 + a_1 \sin^2(\theta) + a_2 \cos^2(\theta)}$$



Known Points **P1, P2**

$$a_1 = \left( \frac{G_c(90^\circ)}{g_c} \right)^2 - 1 \quad a_2 = \left( \frac{G_c(0^\circ)}{g_c} \right)^2 - 1$$

# Application to off-axis tests

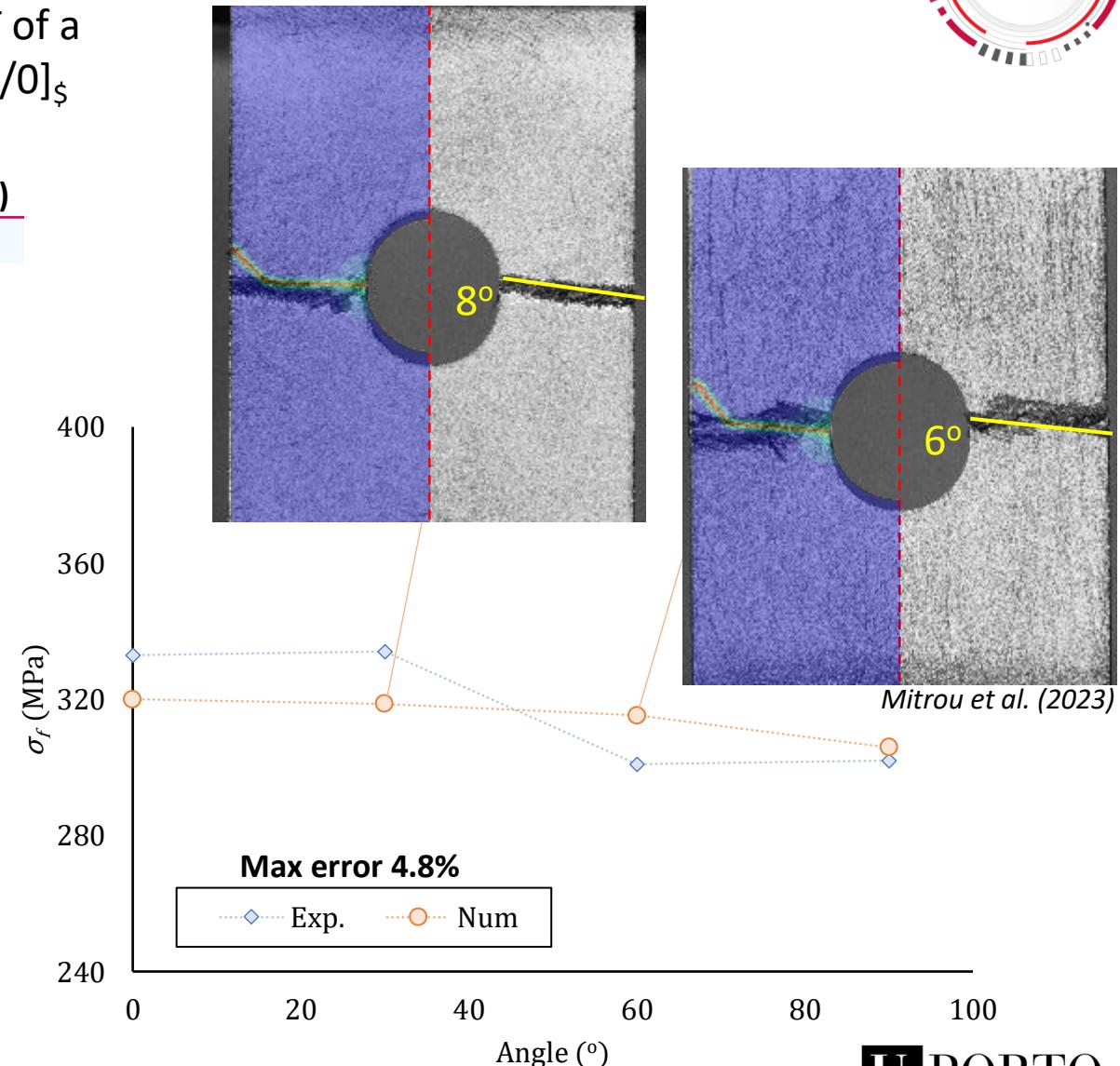
Experimental results from [Furtado et al. \(2021\)](#) for the off-axis OHT of a hard thin-ply laminate of lay-up: [45/-45/0/45/-45/90/0/45/-45/90/0]<sub>§</sub>

	$E_x$ (GPa)	$E_y$ (GPa)	$G_{xy}$ (GPa)	$\nu_{xy}$	$G_c^{0^\circ}$ (N/mm)
Lamina	146.6	8.7	4.6	0.34	67
Laminate	54.0	48.3	4.6	0.39	19.7

Scaling constants:  $a_1 = -0.9171$ ,  $a_2 = -0.9399$

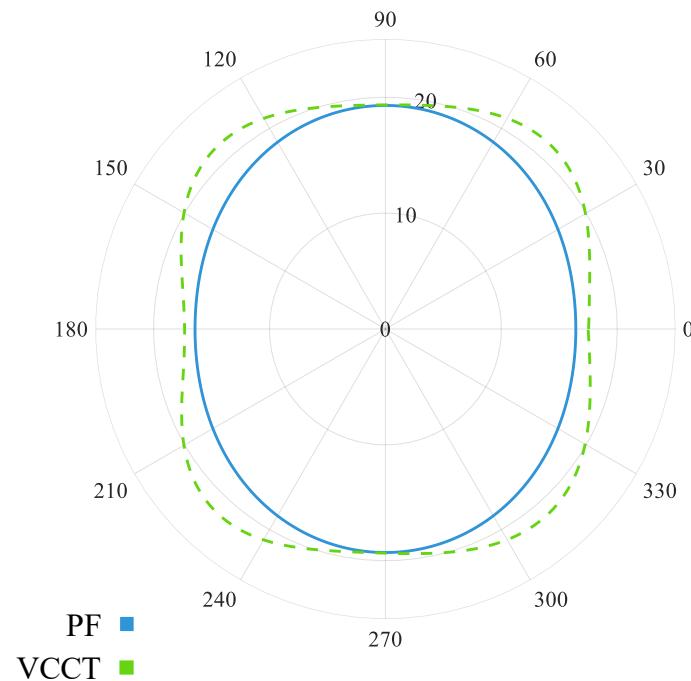
	Exp. Av.	FEA Prediction	Error (%)
On-axis ( $0^\circ$ )	333.00	319.98	4.07
$30^\circ$	334.00	318.62	4.83
$60^\circ$	301.00	315.20	-4.51
$90^\circ$	302.00	305.87	-1.27

Values of strength in MPa



# But...

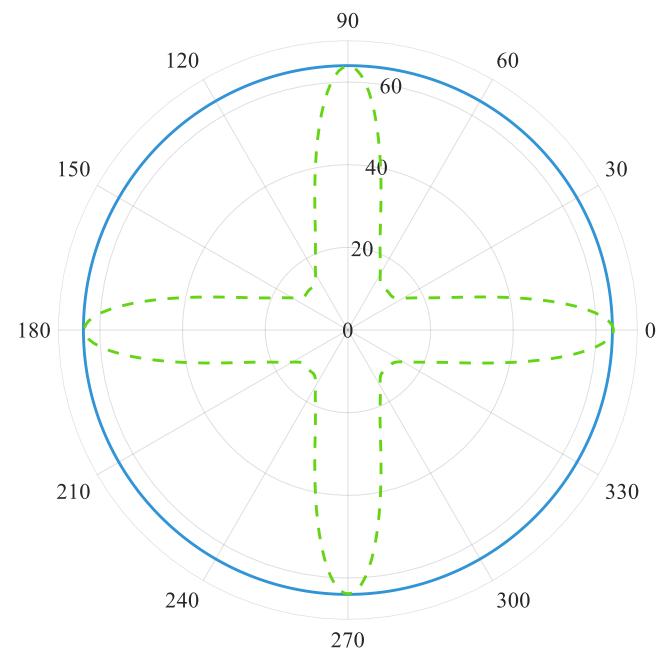
The accurate predictability for the off-axis MD OHT seems be linked to the **weak level** of anisotropy the plate has:



*Assuming the SERR distribution is a valid indicator of a fracture toughness distribution*

What is to be expected in **strongly anisotropic plates**?

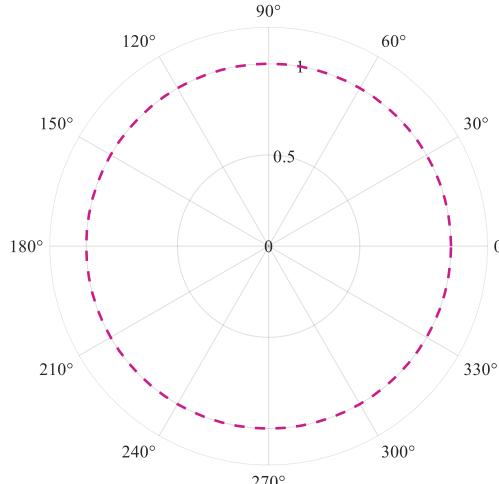
e.g., the cross-ply...



*There is a discrepancy in most angles*

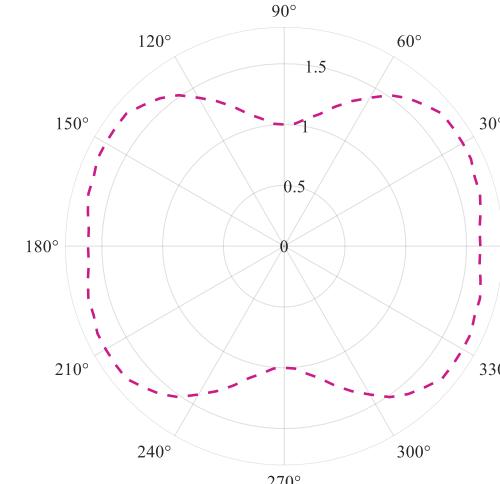
# Testing for validation...

**QI** -  $[90, -45, 0, 45]_{4s}$

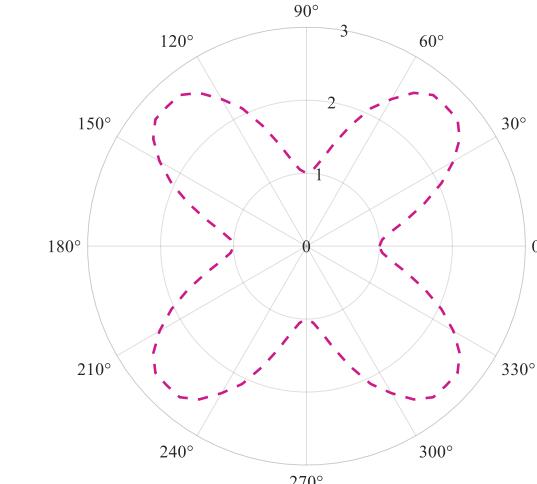


Weakest

**H30** -  $[90, 0, \pm 30, 0, 90, \pm 30]_{2s}$

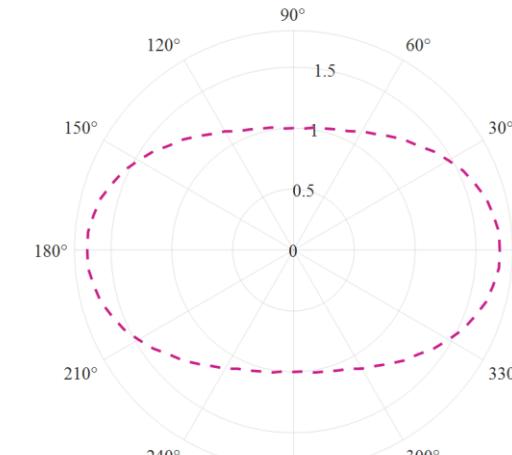


**H1575** -  $[90, \pm 75, 0, \pm 15, 0, 90]_{2s}$



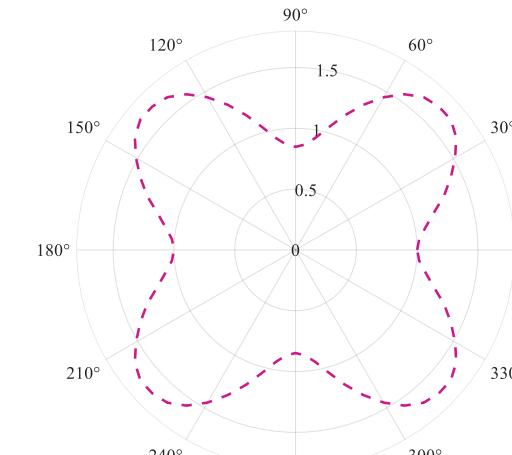
Strongest

**SOFT** -  $[90, \pm 45, 90, \pm 45, 90, 0]_{2s}$

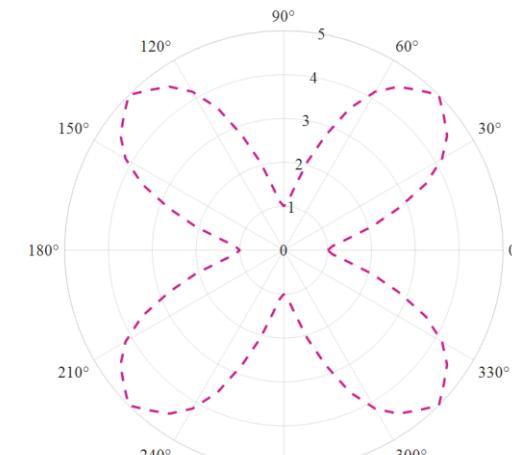


■  $1/G_c(\theta)$

**H6015** -  $[90, \pm 60, 0, \pm 15, 90, 0]_{2s}$



**CP** -  $[90, 0]_{8s}$



# The soft one

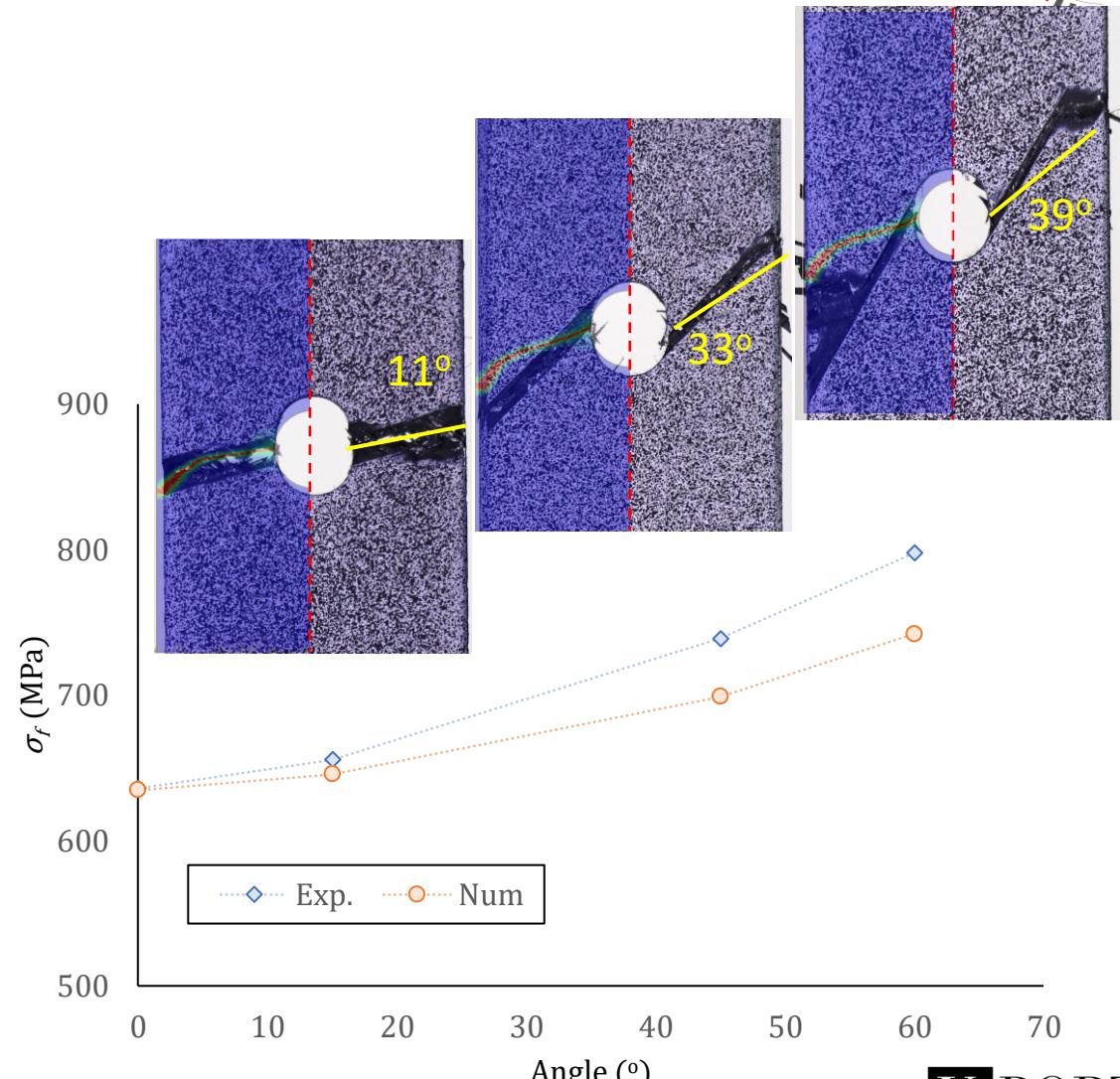
Experimental results for the off-axis OHT of a “soft” thin-ply laminate of lay-up:  $[90/\pm 45/90/\pm 45/90/0]_{2s}$  for T800-736LT from NTPT

Lamina	$E_x$ (GPa)	$E_y$ (GPa)	$G_{xy}$ (GPa)	$\nu_{xy}$	$G_c^{0^\circ}$ (N/mm)
	143.8	7.85	4.6	0.38	171

Scaling constants:  $a_1 = -0.9657$ ,  $a_2 = -0.8382$

	Exp. Av.	FEA Prediction	Error (%)
On-axis ( $0^\circ$ )	635.89	634.51	-0.22
15°	655.56	645.45	-1.54
45°	738.75	698.745	-5.42
60°	797.51	741.7	-7.00

Values of strength in MPa



# The H30

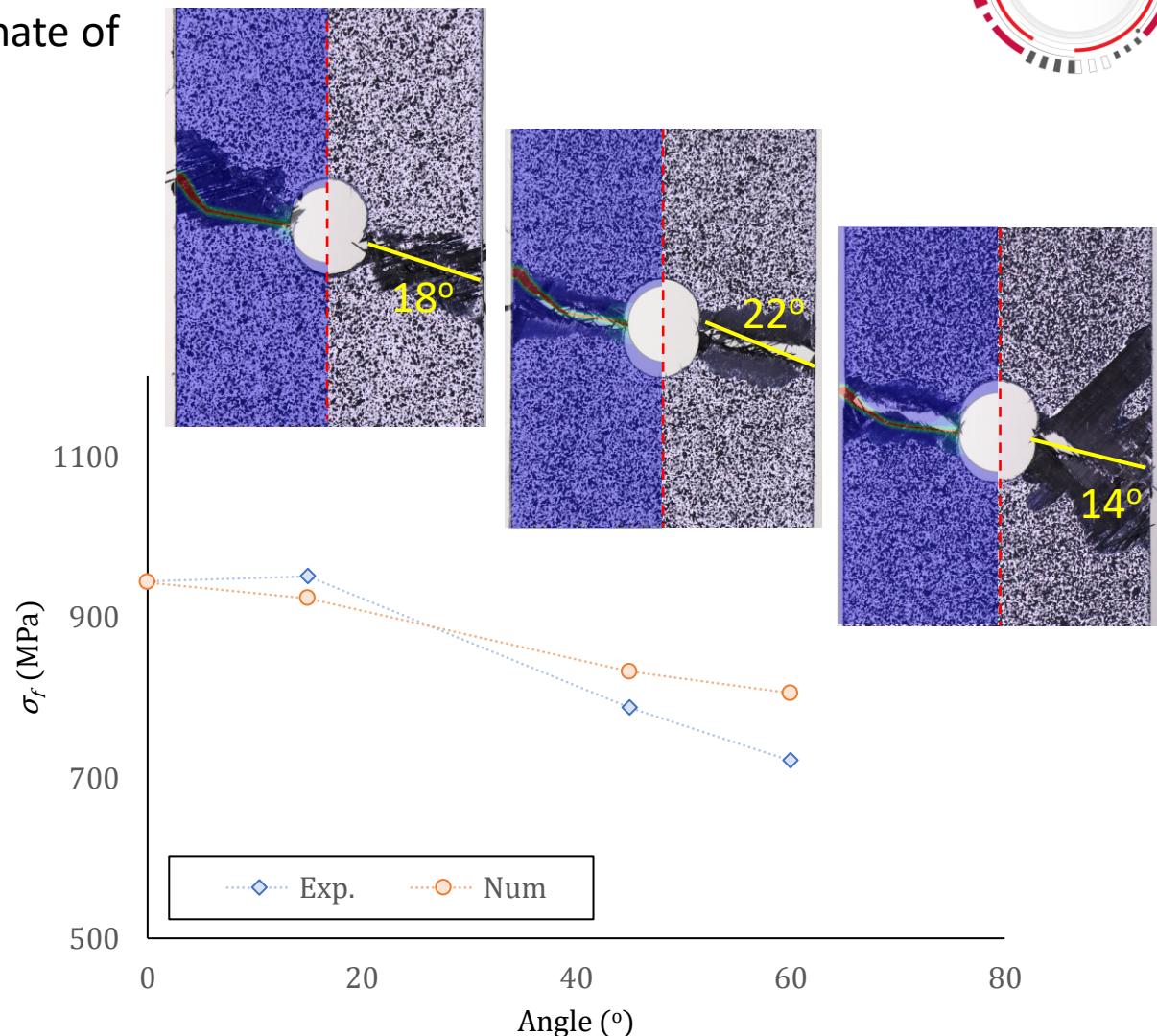
Experimental results for the off-axis OHT of a “hard” thin-ply laminate of lay-up: [90/ $\pm 30/0/90/\pm 30]_{2s}$  for T800-736LT from NTPT

Lamina	$E_x$ (GPa)	$E_y$ (GPa)	$G_{xy}$ (GPa)	$\nu_{xy}$	$G_c^{0^\circ}$ (N/mm)
	143.8	7.85	4.6	0.38	171

Scaling constants:  $a_1 = -0.8332$ ,  $a_2 = -0.9330$

	Exp. Av.	FEA Prediction	Error (%)
On-axis ( $0^\circ$ )	944.52	943.065	-0.15
15°	950.82	923.38	-2.89
45°	787.13	831.995	5.70
60°	721.61	805.18	11.58

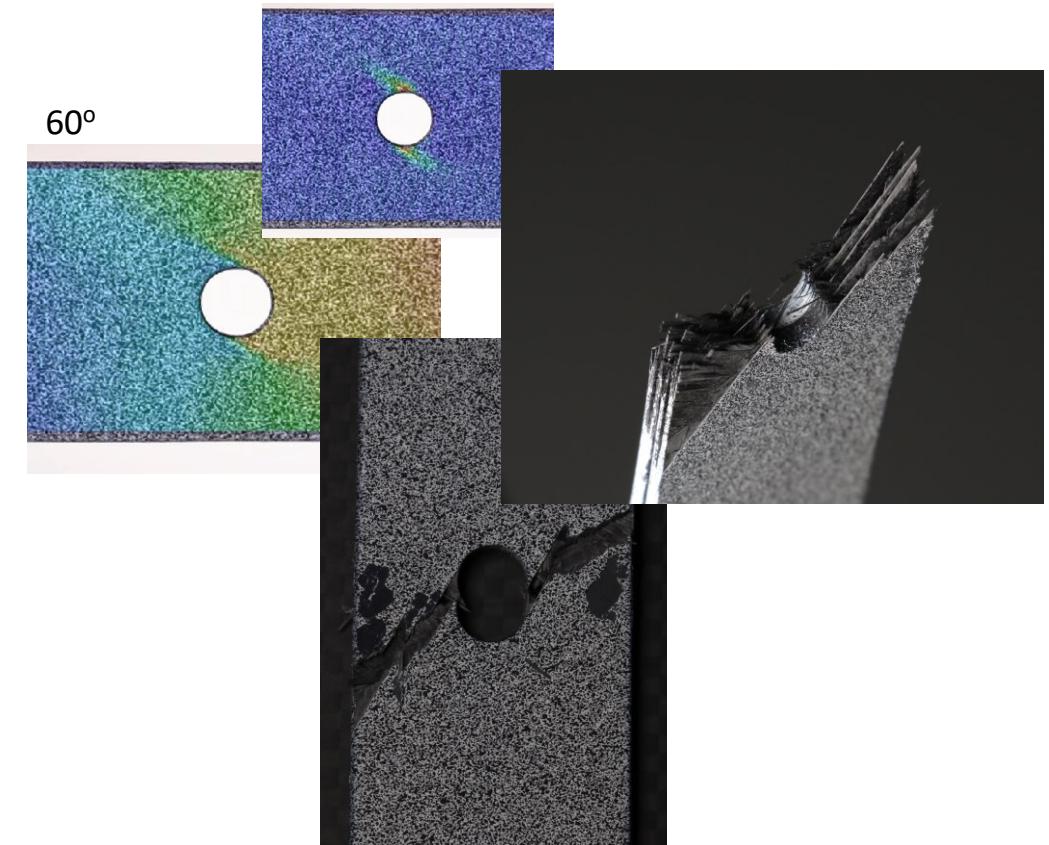
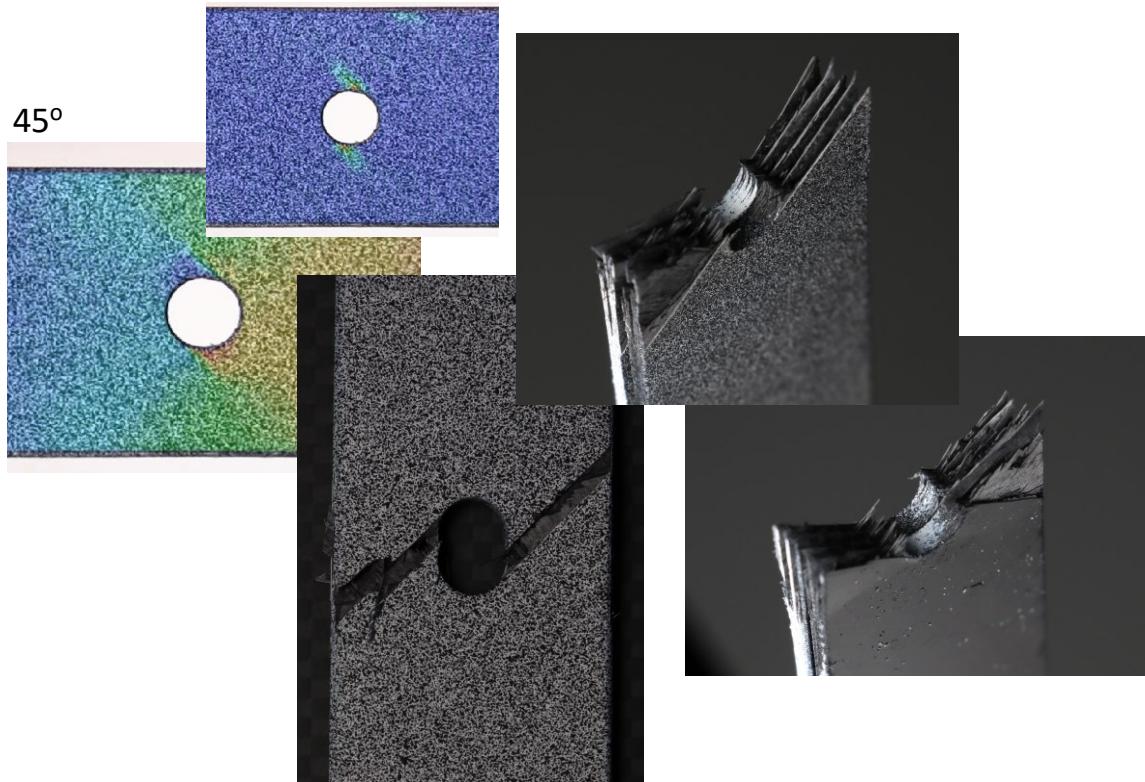
Values of strength in MPa



# The rest...

In fact, things get a bit more complicated...

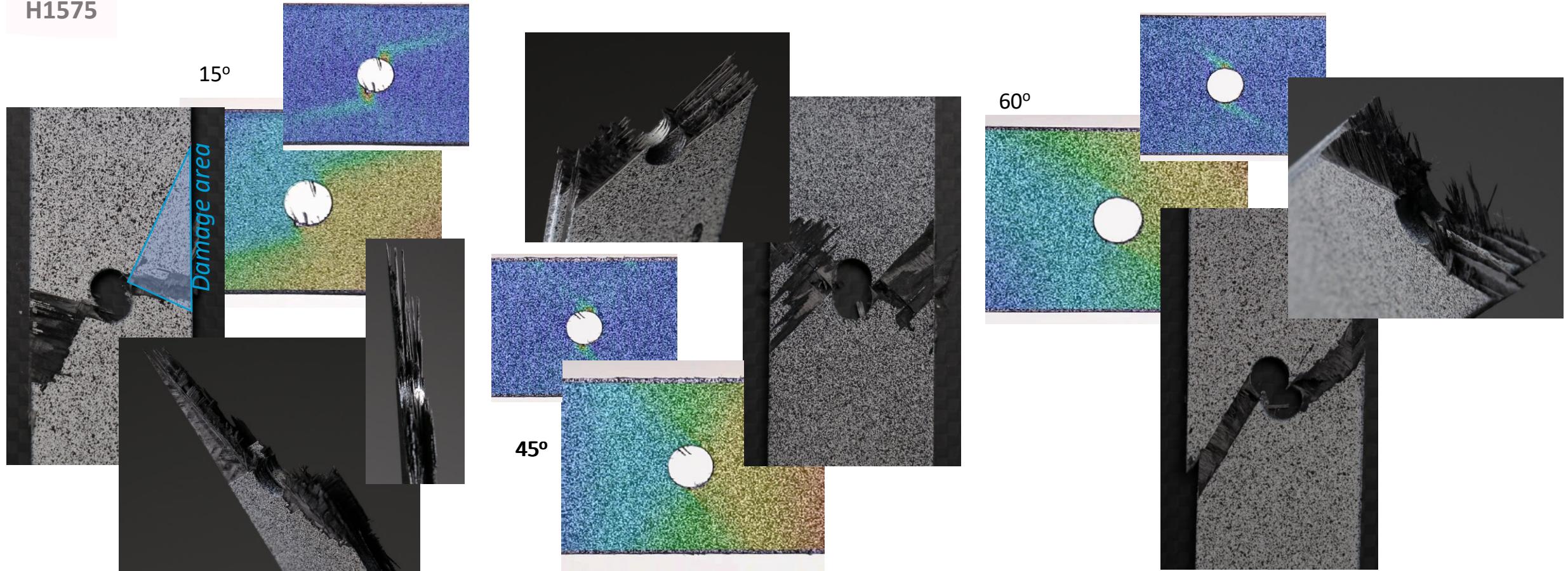
H6015



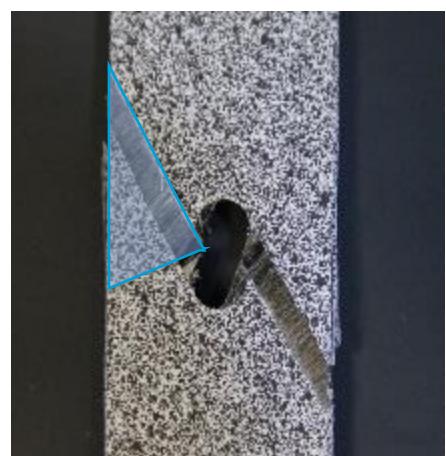
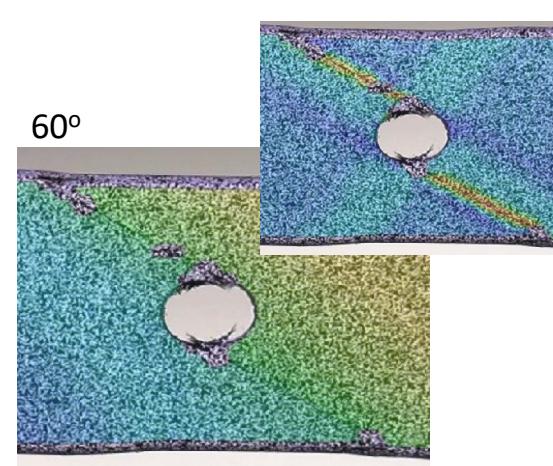
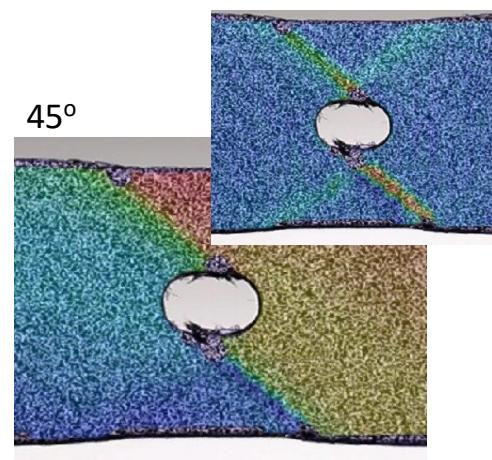
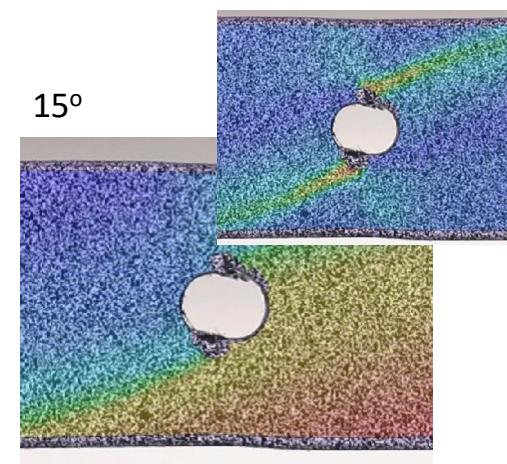
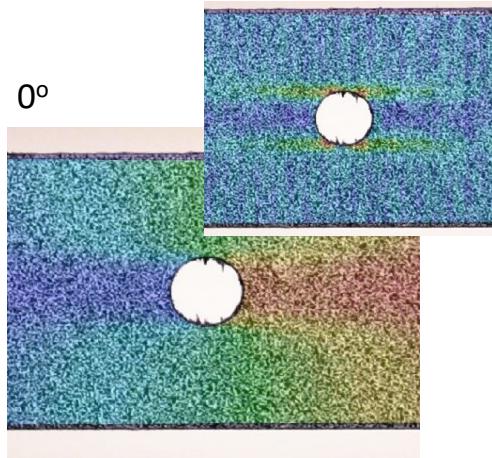
# The rest...

In fact, things get a bit more complicated...

H1575



# The CP



## Conclusions

- A PF ESL approach can be used to successfully predict **off-axis** notched strengths of MD thin-ply laminates residing in the weakly anisotropic range.
- There is a clear dependence of the overall behavior of MD thin-ply laminates to the level of anisotropy they exhibit

as for what follows...

- Continue exploring and developing methods and tools....



For listening up to here...

Thank you !

Contact: [anatomitrou@fe.up.pt](mailto:anatomitrou@fe.up.pt)



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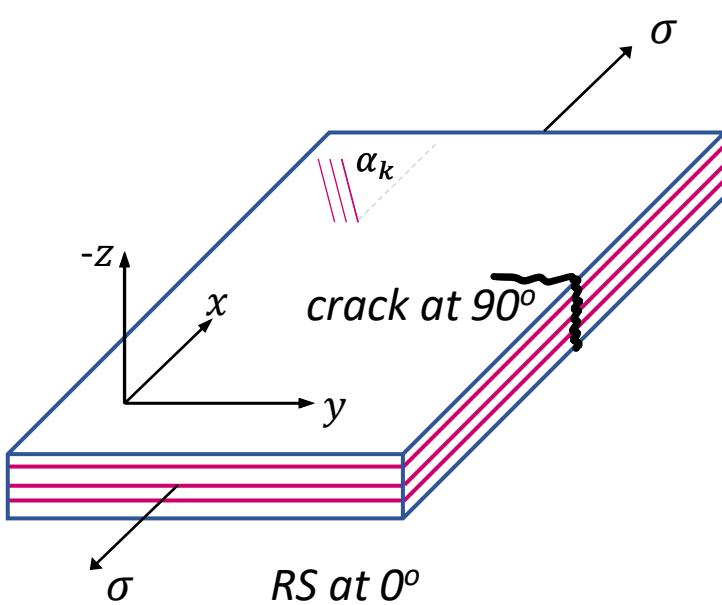
31/07/2023



# Directional Toughness

The toughness of a MD laminate can be determined by using as an input  
Camanho and Catalanotti (2011):

- Lay-up of the laminate
- Toughness of the  $0^\circ$  ply



$$G_c^L = \sum_{k=1}^n G_c^k v_k = \dots = G_c^0 E_{eq}^0 \sum_{k=1}^n \left( \Omega_k \frac{\chi_k}{\chi_0} \right)^2 \frac{v_k}{E_{eq}^k}$$

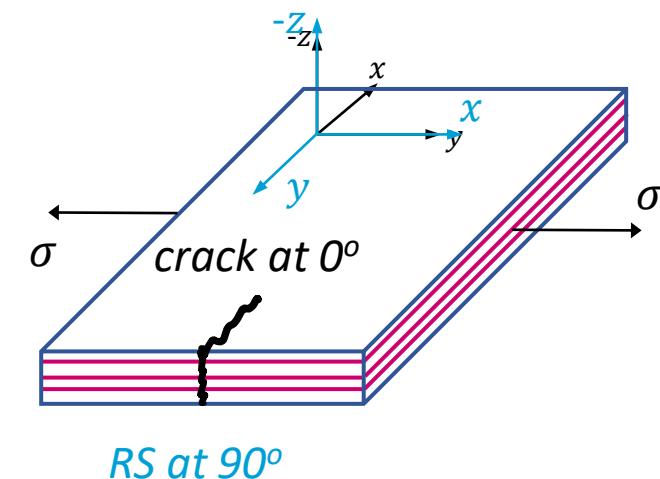
*number of balanced sub-laminates*

**Scaling constants:**

$$a_1 = \left( E_{eq}^0 \sum_{0^\circ} \left( \Omega_k \frac{\chi_k}{\chi_0} \right)^2 \frac{v_k}{E_{eq}^k} \right)^2 - 1$$

$$a_2 = \left( E_{eq}^0 \sum_{90^\circ} \left( \Omega_k \frac{\chi_k}{\chi_0} \right)^2 \frac{v_k}{E_{eq}^k} \right)^2 - 1$$

*Essentially the Lay-up definition is changes to reflect a  $90^\circ$  rotation of the plies*



# VCCT technique for ERR distribution

Run the model until a certain  $u$  is reached and record the ERR11 and ERR12 components.

*Loop for all possible angles  $\theta$  of the material system*

Given a known  $G_c(0^\circ)$  it scales the respective ERR11 value to obtain the  $G_c(\theta)$  distribution

